# Electrical conductivity of Cr<sub>2</sub>O<sub>3</sub>-doped Y<sub>2</sub>O<sub>3</sub>-stabilized ZrO<sub>2</sub>

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The electrical conductivity of  $Cr_2O_3$ -doped  $Y_2O_3$ -stabilized  $ZrO_2$  (YSZ) has been studied as functions of composition, temperature and oxygen pressure. The specimens have been prepared by hot pressing of co-precipitated oxides to yield >99.7% density. The  $Cr_2O_3$  added above the solubility limit ( $\approx 0.7 \text{ mol }\%$ ) precipitated as a secondary phase at the grain boundaries. The conductivity of  $Cr_2O_3$ -doped YSZ was almost independent of the oxygen pressure in the range  $10^{18}$  to  $10^5$  Pa, indicating a dominant ionic condition. The electronic conductivity of dopant  $Cr_2O_3$  would be hindered by the higher ionic conductivity in the  $p_{O_2}$  ranges studied. The conductivity and the activation energy for conduction decreased slightly with the addition of  $Cr_2O_3$ . These phenomena seemed to be caused by vacancy trapping or polarization at the grain boundaries with the  $Cr_2O_3$  precipitates. The samples with 1 mol %  $Cr_2O_3$  added to zirconia containing various  $Y_2O_3$  contents showed similar conduction behaviour to those without  $Cr_2O_3$  addition; that is, the conductivity maxima are observed at around 8 mol %  $Y_2O_3$  addition to zirconia, and the activation energies increased with the  $Y_2O_3$  addition.

#### 1. Introduction

It is generally accepted that stabilized  $ZrO_2$  is a defect solid solution with oxygen vacancies [1, 2] and electrical conduction occurs due to the mobility of oxygen ions at higher temperatures. This ionic conductivity has led to the applications of stabilized  $ZrO_2$  in galvanic cells, oxygen sensors, fuel cells, etc. Among ZrO<sub>2</sub> electrolytes Y<sub>2</sub>O<sub>3</sub>-stabilized ZrO<sub>2</sub> is considered to be better than CaO- or MgO-stabilized ZrO<sub>2</sub>, in view of its higher conductivity and the stability over a wide temperature range. A maximum conductivity for Y<sub>2</sub>O<sub>3</sub>stabilized  $ZrO_2$  has been reported by Dixon *et al.* [3] and Strickler and Carlson [4] at the cubic-tetragonal phase boundary (8 to  $9 \mod \% Y_2O_3$ ). Furthermore the conductivity of Y2O3-stabilized ZrO2 remains constant, exhibiting pure ionic conductivity over a wide range of oxygen partial pressures [5].

Studies on the conductivity of stabilized ZrO<sub>2</sub> with various additives have been of interest to investigators for the applications of stabilized  $ZrO_2$  in sensors [6], mixed conductors [7, 8], etc. The mixed conductors obtained from  $Y_2O_3$ -stabilized ZrO<sub>2</sub> are excellent conductors for hydrogen production from steam and for rechargeable batteries. Anthony [9] and Browall and Doremus [8] reported that Cr<sub>2</sub>O<sub>3</sub>-doped Y<sub>2</sub>O<sub>3</sub>stabilized ZrO<sub>2</sub> is one of the most promising mixed conductors in hydrogen production. They measured the a.c. conductivity and transference number for Cr<sub>2</sub>O<sub>3</sub>-doped Y<sub>2</sub>O<sub>3</sub>-stabilized ZrO<sub>2</sub> and reported a transference number of about 0.8 at 1000°C and  $10^{-16}$  atm  $p_{0,2}$ . Karavaev et al. [10] also have reported electrical conductivity and transference numbers for materials in the  $ZrO_2 - Y_2O_3 - Cr_2O_3$  system. However, these studies were limited to the transference number

and conductivity measurement with temperature and they did not report the variation of conductivity with  $p_{O_2}$  and composition. Thus in the present study it was intended to measure the conductivity of  $Cr_2O_3$ -doped  $Y_2O_3$ -stabilized  $ZrO_2$  with oxygen partial pressure, temperature and composition using pore-free samples prepared by hot pressing.

Previously we studied the phase relations in the system  $ZrO_2 - Y_2O_3 - Cr_2O_3$  [11] and found that  $Cr_2O_3$  is compatible with a  $ZrO_2$  solid solution containing  $\approx 17 \text{ mol }\% Y_2O_3$ . Again in a hot-pressing study [12] the solubility of  $Cr_2O_3$  in 8 mol %  $Y_2O_3$ -stabilized  $ZrO_2$  was found to be 0.7 mol % at 1450° C. The present paper describes the conductivity measurements of the materials in the system  $ZrO_2 - Y_2O_3 - Cr_2O_3$ .

### 2. Experimental procedure

#### 2.1. Samples

The samples for conductivity measurements were prepared by the hot pressing of co-precipitated materials. The details of starting powder preparation and hotpressing technique have been described in a previous paper [12]. All the samples for conductivity measurement were hot-pressed under the same condition at  $1500^{\circ}$  C, with 43.7 MPa pressure for 30 min in an argon atmosphere using graphite dies. Pellets of 10 mm diameter and 3 to 4 mm height were obtained by hot pressing. They were annealed first at  $1200^{\circ}$  C for 48 h in air to oxidize all contaminants from the die and metallic chromium produced by the reduction of  $Cr_2O_3$  during hot pressing. Specimens of about  $1.5 \text{ mm} \times 2.5 \text{ mm} \times 9 \text{ mm}$  were then cut from those pellets to be used in conductivity measurements.

The density of hot-pressed samples was measured

by Archimedes' method in mercury. Microstructural observations were done for the polished and etched (in boiling  $H_3PO_4$ ) surfaces using scanning electron microscopy (SEM).

#### 2.2. D.c. conductivity measurement

The d.c. four-probe method [13] was used for d.c. conductivity measurement. Platinum wires of 0.2 mm diameter were connected to the specimen as electrical probes through pressure contact. To eliminate the effect of surface currents, platinum paste was applied to both edge probes which were used to apply the current. Potential difference was measured between the central probes. The circuit used for conductivity measurement is shown in Fig. 1. The current through the specimen was measured by the ohmic drop across the standard resistor of 100 or  $1000 \Omega$ . All the voltages were measured with a high-impedance digital voltmeter. During the conductivity measurement, the specimen was suspended horizontally in a vertical tube furnace with an SiC double spiral heating element by means of four probes supported by an alumina holder. The temperature was measured by a Pt/Pt-13 Rh thermocouple calibrated to the melting points of palladium and gold and controlled within 1°C.

Oxygen partial pressure was controlled by  $H_2/CO_2$ gas mixtures or by an  $O_2$  pump. Partial oxygen pressure was measured by a zirconia oxygen sensor placed downstream of the furnace. The e.m.f. developed between both sides of the sensor as a result of  $p_{O_2}$ difference is

$$E = \frac{RT}{4F} \ln \frac{p_{O_2}}{p_{O_2 \text{ref.}}}$$

where R = gas constant, T = temperature, F = Faraday constant, and  $p_{O_2}$ ,  $p_{O_2\text{ref.}}$  are the partial oxygen pressures in measured and reference gases, respectively. Air is used as the reference gas. The  $p_{O_2}$  at the specimen  $T = T_{\text{specimen}}$  was obtained from the  $p_{O_2}$  at the sensor  $T = T_{\text{sensor}}$  on calculations based upon the thermodynamical equilibrium constants [14] for each reaction between the gases in the gas mixture.





Figure 1 Electrical circuit and specimen for d.c. conductivity measurement.  $\sigma = d/abR$ .

#### 2.3. Complex impedance measurement

The complex impedance of  $Cr_2O_3$ -doped YSZ was measured using a vector impedance meter. Annealed hot-pressed specimens of 10 mm diameter were used. Firstly platinum paste was applied to both sides and fired at 800° C. Then they were placed between two platinum electrodes of the equipment. The impedance and phase angle for various frequencies were read by direct meter readings at various temperatures.

#### 3. Results and discussion

The densities and grain sizes of the samples used for conductivity measurements are given in Table I. All the samples had 99% of theoretical density and 1 to  $9\,\mu m$  grain sizes. The microstructures of the specimens showed secondary phase particles precipitated on the grain boundaries in samples containing more than 1 mol % Cr<sub>2</sub>O<sub>3</sub>. By energy-dispersive spectroscopy, these secondary-phase particles were found to be  $Cr_2O_3$  precipitates. The microstructure and  $CrK\alpha$ X-ray image for a  $3 \mod \%$  Cr<sub>2</sub>O<sub>3</sub>-doped sample is shown in Fig. 2. The secondary  $Cr_2O_3$  phase can be seen in white among dark ZrO2 solid-solution grains in Fig. 2. The microstructures and CrKa X-ray images showed homogeneous Cr<sub>2</sub>O<sub>3</sub> dispersion all over the specimen in addition to the precipitates on the grain boundaries.

#### 3.1. Conductivity behaviour

The ohmic behaviour of the electrical conductivity was examined by changing the d.c. current from 0.6 to  $15 \text{ mA cm}^{-2}$ . Potential differences between each pair of probes were measured to examine the potential drop along the specimen. Almost all the results showed ohmic behaviour, but some cases exhibited a non-ohmic potential drop along the specimen. When log [ $p_{O_2}$ (Pa)] was around zero such non-ohmic behaviour could generally be observed. As an example, Fig. 3 shows the observed potential differences in a CO<sub>2</sub> atmosphere. It shows a non-proportional relation between potential drop and the current at the cathode for both normal and reverse currents. The cathode process is represented by the reaction

$$2e' + \frac{1}{2}O_2 + V_o'' = O_o$$

Thus it seems the cathode polarization occurs due to a very slow reaction at the cathode in low  $p_{O_2}$ . However, potential differences between the two middle probes showed linearity with current for both normal and reverse directions. This non-ohmic behaviour

TABLE I Density and grain sizes of the samples used for conductivity measurement,  $(1 - y)[(1 - x)ZrO_2 + xY_2O_3] + yCr_2O_3$ ; samples hot-pressed at 1500° C under 43.7 MPa pressure for 30 min

| Composition |   | Density | Average grain |
|-------------|---|---------|---------------|
| x           | y | (%)     | size (µm)     |
| 8           | 0 | 99.8    | 9             |
| 8           | 1 | 99.9    | 8             |
| 8           | 3 | 99.9    | 8             |
| 5           | 1 | 99.9    | 1             |
| 12          | 1 | 99.9    | 4             |
| 15          | 1 | 98.5    | 3             |
| 17          | 1 | 99.0    | 7             |



Figure 2 (a) Microstructure and (b) CrKa X-ray image for hot-pressed 3 mol % Cr<sub>2</sub>O<sub>3</sub>-doped YSZ.

was observed only in the regions of log  $[p_{O_2}(Pa)]$ around zero. In  $p_{O_2}$  of both very low and very high values, potential differences did not exhibit such a non-ohmic behaviour and conductivity data could be obtained in those regions from the plot of potential difference against current.

#### 3.2. Variation of conductivity with $p_{0_2}$

Electrical conductivity dependence on  $p_{O_2}$  was examined for 8 mol %  $Y_2O_3$ -stabilized ZrO<sub>2</sub> containing 0 to 3 mol % Cr<sub>2</sub>O<sub>3</sub>. The conductivity results plotted against  $p_{O_2}$  are shown in Fig. 4. The conductivities with  $p_{O_2}$  seem to be almost constant. Although they showed some fluctuations they did not show a significant and systematic slope compared to the slope of 3/16 which was relevant to the conductivity of Cr<sub>2</sub>O<sub>3</sub>. Therefore these fluctuations are considered to be due to experimental errors caused mainly by polarization. Thus the conductivity of Cr<sub>2</sub>O<sub>3</sub>-doped YSZ seems to be almost ionic in the  $p_{O_2}$  range studied.

Arrhenius plots of the conductivity in air are shown.



Figure 3 Potential differences between each pair of probes of the sample at  $1100^{\circ}$  C ( $1 \mod \%$  Cr<sub>2</sub>O<sub>3</sub> doped YSZ, in CO<sub>2</sub>), indicating cathode polarization in this atmosphere.

in Fig. 5. It shows a slight decrease in the conductivity of YSZ on  $Cr_2O_3$  addition. This conductivity decrease may be attributed to the microstructural change on  $Cr_2O_3$  addition. The particles of  $Cr_2O_3$  precipitated on the grain boundaries in these specimens, as seen in Fig. 2. The existence of a secondary phase on the grain boundary generally hinders the ionic conductivity of electrolytes. The  $Cr_2O_3$  precipitated on the grain boundary might have hindered the ionic conduction at the grain boundaries. Since  $Cr_2O_3$  is not an ionic conductor, vacancy trapping or polarization might occur at the grain boundaries. Hence the grain boundary resistivity has been increased with  $Cr_2O_3$  addition.

Furthermore, Fig. 5 shows that the activation energy for conductivity decreased with  $Cr_2O_3$  addition. Activation energies for conductivities were found to be 0.96, 0.93 and 0.90 eV for 0, 1 and 3 mol %  $Cr_2O_3$ added to YSZ, respectively.

## 3.3. Variation of conductivity with composition

The conductivities of 1 mol % Cr<sub>2</sub>O<sub>3</sub>-doped YSZ containing various Y2O3 contents were measured at various temperatures. Fig. 6 shows isothermal conductivities plotted against Y2O3 contents and Fig. 7 shows Arrhenius plots of these conductivities. They show that the conductivity increases with  $Y_2O_3$  to a maximum conductivity at about 8 mol % Y<sub>2</sub>O<sub>3</sub> content and then it decreases with further increasing  $Y_2O_3$ content due to vacancy clustering. Even for pure YSZ a maximum conductivity has been reported in previous studies [4] at compositions of about 8 to 9 mol %  $Y_2O_3$ . Thus the variation of the ionic conductivity behaviour of Cr<sub>2</sub>O<sub>3</sub>-doped YSZ with Y<sub>2</sub>O<sub>3</sub> content was similar to that of pure YSZ. The activation energies for conductivity also increased with increasing  $Y_2O_3$  content. The activation energies for  $1 \mod \%$  $Cr_2O_3$  added to YSZ were found to be 0.86, 0.93, 1.07, 1.09 and 1.23 eV for 5, 8, 12, 15 and 17 mol % Y<sub>2</sub>O<sub>3</sub> compositions, respectively.

The oxygen vacancy concentrations of these specimens were proportional to the stabilizer  $(Y_2O_3)$  content in the solid solution. Therefore ionic conduction increases with  $Y_2O_3$  content at the start. But when the vacancy concentration becomes higher vacancies tend to cluster or become ordered. Because of this the conductivity decreased when the stabilizer content



Figure 4 Conductivity dependency on  $p_{O_2}$ . Open symbols and solid lines for 1 mol %  $Cr_2O_3$ ; filled symbols and broken lines for 3 mol %  $Cr_2O_3$  doped YSZ.

increased beyond the maximum amount required to stabilize the cubic phase. Thus in the present study for  $Cr_2O_3$ -doped YSZ also the conductivity decreased with an increase of activation energy due to clustering and/or ordering of vacancies when the  $Y_2O_3$  content exceeded 8 mol%.

#### 3.4. Complex impedance

Complex impedance was measured for  $3 \mod \% \operatorname{Cr}_2O_3$ added to an  $8 \mod \% \operatorname{Y}_2O_3$ -stabilized ZrO<sub>2</sub> sample at the temperatures 224, 280 and  $310^{\circ}$  C. Impedence plots are shown in Fig. 8. In this case, however, the use of platinum paste did not give a porous electrode surface, so a high resistance was created at the electrode. Thus the results did not distinguish the bulk and grain-boundary resistivities, which was considered to be an effect of the non-porous electrode.



Figure 5 Conductivity of  $Cr_2O_3$ -doped YSZ with reciprocal temperature. D.c. values: (O) 0%, ( $\triangle$ ) 1%, ( $\Box$ ) 3%  $Cr_2O_3$ ; a.c. values ( $\blacksquare$ ) 3%  $Cr_2O_3$ ; (---) data from Browall and Doremus [8] for 2%  $Cr_2O_3$ .

However, the first arcs drawn on the d.c. conductivity data agree approximately with these impedance results.

#### 3.5. Defect structure and electrical conductivity

Electrical conductivity in solid electrolytes is primarily determined by the presence of lattice defects [12, 13] whose concentration and mobility are important parameters. Therefore a knowledge of various types of defect such as ionic and electronic is essential to explain the conductivity behaviour.

#### 3.5.1. Stabilized ZrO<sub>2</sub>

When  $Y_2O_3$  is added to  $ZrO_2$ ,  $Y^{3+}$  ions substitute to the lattice sites of  $Zr^{4+}$  creating oxygen vacancies. The reaction can be written as

$$Y_2O_3 \xrightarrow{ZrO_2} 2Y'_{Zr} + V_0'' + 3O_o \qquad (1)$$

In the intermediate  $p_{O_2}$  range, the vacancy concentration is determined by the impurity  $(Y_2O_3)$  content and it is much larger than that of the other defects. Therefore the conduction through oxygen



Figure 6 Variation of isothermal conductivity of  $1 \mod \% \operatorname{Cr}_2\operatorname{O}_3$ -doped YSZ with  $\operatorname{Y}_2\operatorname{O}_3$  content.



Figure 7 Variation of conductivity of  $1 \mod \% \operatorname{Cr}_2O_3$ -doped ZrO<sub>2</sub> stabilized with various  $Y_2O_3$  contents with reciprocal temperature. Content of  $Y_2O_3$ : ( $\bigcirc$ ) 5%, ( $\bigcirc$ ) 8%, ( $\triangle$ ) 12%, ( $\triangle$ ) 15%, ( $\square$ ) 17%.

ions is usually independent of  $p_{O_2}$ . However the ZrO<sub>2</sub> becomes oxygen-deficient depending on the  $p_{O_2}$  and temperature as follows [15]:

$$O_o = \frac{1}{2}O_2 + V_o'' + 2e'$$
 (2)

The equilibrium constant  $K_1$  for this reaction is given by

$$K_1 = [V_0^{\cdot \cdot}] [e']^2 p_{O_2}^{1/2}$$

But  $[V_o^{++}] = \frac{1}{2}[Y'_{Zr}]$  is almost constant according to Equation 1, and therefore

$$[e'] = K'_1 p_{O_2}^{-1/4}$$
(3)



Figure 8 Complex impedence plot for 3 mol % Cr2O3-doped YSZ.

Thus at high temperature and low  $p_{O_2}$ , n-type conductivity proportional to  $p_{O_2}^{-1/4}$  is added to ionic conductivity.

Similarly in very high  $p_{O_2}$ , excess oxygen may enter in the place of V<sub>o</sub><sup>•</sup> creating h<sup>•</sup> through the reaction

$$\frac{1}{2}O_2 + V_o^{..} = O_o + 2h^{..}$$
 (4)

The equilibrium constant  $K_2$  for this reaction is given by

$$K_2 = \frac{[h^{\cdot}]^2}{[V_o^{\cdot}] p_{O_2}^{1/2}}$$
  
As  $[V_o^{\cdot \cdot}] = [Y'_{Zr}] = \text{constant},$ 

$$[h'] = K'_2 p_{O_2}^{1/4}$$
 (5)

Thus at very high  $p_{O_2}$ , it is possible that conductivity occurs through electron holes [h ] and this conductivity will be proportional to  $p_{O_2}^{1/4}$ . However, these electronic conductivities do not appear in ordinary atmospheres in Y<sub>2</sub>O<sub>3</sub>-stabilized ZrO<sub>2</sub>; they then have almost constant electrical conductivity and it is dominated by the oxygen ion vacancies over a wide range of  $p_{O_2}$ .

#### $3.5.2. Cr_2O_3$

Pure  $Cr_2O_3$  has p-type conductivity [16] caused by excess oxygen through the reaction

$$\frac{3}{2}O_2 = 3O_0 + 2V_{Cr}'' + 6h^{\circ}$$
 (6)

The equilibrium constant  $K_3$  for this reaction is given by

$$K_3 = \frac{[\mathbf{V}_{Cr}''']^2 [\mathbf{h}^{\cdot}]^6}{p_{O_2}^{3/2}}$$

and, since  $3[V_{Cr}'''] = [h]$ ,

$$[h^{\cdot}] = K'_{3} p_{O_{2}}^{3/16}$$
(7)

Thus the electrical conductivity of pure  $Cr_2O_3$  is p-type and proportional to  $p_{O_2}^{3/16}$ .

#### 3.5.3. $Cr_2O_3$ -doped YSZ

When  $Cr_2O_3$  is added to YSZ,  $Cr^{3+}$  ions can enter the structure of  $Zr_{1-x}Y_xO_{2-x/2}$ , either by substitution for cations in the cation sublattice or by taking interstitial positions. In the case of substitution, it forms oxygen vacancies as follows:

$$Cr_2O_3 = 2Cr'_{Zr} + V_o^{-1} + 3O_o$$
 (8)

and in the case of interstitial solution

$$Cr_2O_3 + 3V_o^{...} = 2Cr_i^{...} + 3O_o$$
 (9)

In a previous study [12] a solubility of 0.7 mol %  $Cr_2O_3$  in 8 mol %  $Y_2O_3$ -stabilized  $ZrO_2$  was observed. Further, the lattice parameter of YSZ decreased with  $Cr_2O_3$  addition. For an interstitial solution, the decrease of lattice parameters cannot be considered. If a substitutional solution was considered, the lattice parameter decrease was in agreement with Vegard's law as a result of the smaller cation ( $Cr^{3+}$ , 0.062 nm) substituting for a larger cation ( $Zr^{4+}$ , 0.079 nm). Thus it is assumed that  $Cr_2O_3$  dissolved substitutionally according to the Reaction 8. The  $Cr^{3+}$  ions dissolved in  $ZrO_2$  solid solution may cause a small electronic conductivity as a result of its affinity to change the valence state as a transition-metal ion. Thus two possible defect reactions which cause electronic conductivity can be described as follows:

(a) In the high  $p_{O_2}$  region

$$Cr'_{Zr} + V_o^{\cdot \cdot} + \frac{1}{2}O_2 = O_o + Cr_{Zr} + h^{\cdot}$$
 (10)

where the equilibrium constant is

$$K_4 = \frac{[Cr_{Zr}][h^{\cdot}]}{[Cr'_{Zr}][V_o^{\cdot}]p_{O_2}^{1/2}}$$

Since  $[Cr_{Zr}] = [h^{\cdot}]$  and  $[V_{o}^{\cdot \cdot}] = constant$ ,

$$[h^{\cdot}] = K'_{4}[Cr'_{Zr}]p_{O_{2}}^{1/4}$$
(11)

(b) In the low  $p_{O_2}$  region

$$Cr'_{Zr} + O_o = \frac{1}{2}O_2 + V_o'' + Cr''_{Zr} + e'(12)$$

where the equilibrium constant is

$$K_{5} = \frac{[V_{o}^{"}][Cr_{Zr}^{"}][e']p_{O_{2}}^{1/2}}{[Cr_{Zr}^{'}]}$$

Since  $[Cr''_{Zr}] = [e']$  and  $[V''_o] = constant$ 

$$[e'] = K'_{5}[Cr'_{Zr}]p_{O_{2}}^{-1/4}$$
(13)

Thus the possible electronic conductivities depend on the dissolved  $Cr_2O_3$  content. But the  $Cr_2O_3$  solubility is very small and therefore the electronic conductivity also should be very small compared to the high ionic conductivity caused by high  $V_o$  concentration. However,  $Cr_2O_3$  addition might alter the conductivity



Figure 9 Schematic representation of the conductivity behaviour of Cr<sub>2</sub>O<sub>3</sub>-doped YSZ compared with pure YSZ.

of YSZ by narrowing the range of ionic conductivity as shown schematically in Fig. 9. Since the results of the present study remained almost constant, the present study has been carried out in this narrow ionic conduction region.

However, this conductivity will also be determined by the microstructure. If the added  $Cr_2O_3$  content was so high that  $Cr_2O_3$  particles could be interconnected, then there would be additional electronic conductivity through the  $Cr_2O_3$  secondary phase.

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